

# Two Population Means

$\sigma_1$  and  $\sigma_2$  Known

---

## Confidence Interval:

---

- Final Answer: Lower Value  $< \mu_1 - \mu_2 <$  Upper Value
  - Margin of Error:  $E = \frac{\text{C.I. Upper Value} - \text{C.I. Lower Value}}{2}$
  - Finding Confidence Interval Using TI: STAT > TESTS > 2-SampZInt > ENTER
- 

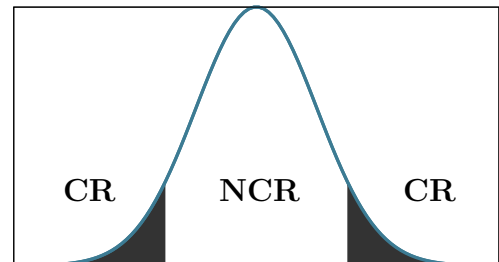
## Hypothesis Testing:

---

### Two-Tail Test:

$$H_0 : \mu_1 = \mu_2$$

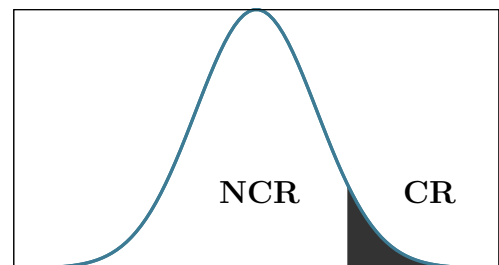
$$H_1 : \mu_1 \neq \mu_2$$



### Right-Tail Test:

$$H_0 : \mu_1 \leq \mu_2$$

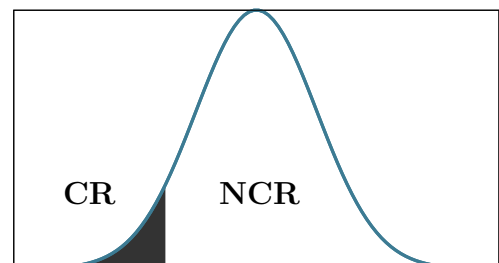
$$H_1 : \mu_1 > \mu_2$$



### Left-Tail Test:

$$H_0 : \mu_1 \geq \mu_2$$

$$H_1 : \mu_1 < \mu_2$$



## Critical Value(s):

- Using TI Calculator

PRGM > ZVAL > ENTER (Twice)

---

## Computed Test Statistic & P-Value:

- Using TI Calculator

STAT > TESTS > 2-SampZTest

- Using formula for C.T.S.:

$$z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

- Using normalcdf( for P-Value:

2ND > VARS > normalcdf( > ENTER

---

Example:

Consider the chart below:

Sample 1	Sample 2
$n_1 = 50$	$n_2 = 40$
$\bar{x}_1 = 84$	$\bar{x}_2 = 80$
$s_1 = \text{Not Given}$	$s_2 = \text{Not Given}$
$\sigma_1 = 6.5$	$\sigma_2 = 7.8$

- Find 99% confidence interval for the difference of two population means.

Solution:

Using 2-SampZInt, we get  $0.04 < \mu_1 - \mu_2 < 7.96$

- Test the claim that  $\mu_1 > \mu_2$ .

Solution:

Here we have  $H_0 : \mu_1 \leq \mu_2, H_1 : \mu_1 > \mu_2$  RTT, Claim

With no  $\alpha$ , using ZVAL, we get C.V.  $Z = 1.645$

Using 2-SampZTest, we get C.T.S.  $Z = 2.600$ , P-Value  $p = .005$

Final Conclusion: Support the Claim